

# Econometrics Test

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Name: \_\_\_\_\_ matricola: \_\_\_\_\_

email: \_\_\_\_\_

1. Say if the following statements are unambiguously true (TRUE), unambiguously false (FALSE) or impossible to classify the way they are stated (CAN'T SAY). Write the motivations to your answers **only** in the space provided. A "CAN'T SAY" answer with no motivations will be considered wrong.

- (a) The rank of the matrix  $C = [1, 2, 3]$  is 1.

TRUE      ☐      FALSE      ☐      CAN'T SAY      ☐

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- (b) An  $n \times n$  identity matrix has rank  $n$ .

TRUE      ☐      FALSE      ☐      CAN'T SAY      ☐

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- (c) A square matrix with  $n$  rows whose elements are all 1 is singular.

TRUE      ☐      FALSE      ☐      CAN'T SAY      ☐

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- (d) The long-run multiplier in a dynamic model can never be negative.

TRUE      ☐      FALSE      ☐      CAN'T SAY      ☐

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- (e) The Godfrey test makes no sense in a cross-section sample.

TRUE      ☐      FALSE      ☐      CAN'T SAY      ☐

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2. A linear model was estimated on 90 observations and 6 explanatory variables yields a sum of squared residual equal to 350; after imposing 3 restrictions, it goes up to 420. Calculate the  $F$  and  $W$  tests, plus the  $R^2$  indices for both models, assuming that the sample variance of the dependent variable is equal to  $\frac{1}{n} \sum_{i=1}^n (y_i - \bar{Y})^2 = 14$

$F$  test: \_\_\_\_\_  $p$ -value: \_\_\_\_\_  
 Decision: ACCEPT ☐ REJECT ☐

$W$  test: \_\_\_\_\_  $p$ -value: \_\_\_\_\_  
 Decision: ACCEPT ☐ REJECT ☐

$R_0^2$ : \_\_\_\_\_  $R_1^2$ : \_\_\_\_\_

3. Suppose the following model was estimated on a sample of households:

$$\hat{c}_i = \beta_0 + \beta_1 n_i + \beta_2 y_i$$

where  $\beta_0 = 1.25$ ,  $\beta_1 = 0.42$  and  $\beta_2 = 0.54$ ;  $c_i$  is the log of the consumption of some good for the whole household,  $n_i$  is the log of the number of household members and  $y_i$  is the log of total household income.

- (a) discuss the economic meaning of the restriction  $R\beta = 1$ , where  $R = [0, 1, 1]$ ;  
 (b) assuming that the estimated covariance matrix is

$$\hat{V} = \begin{bmatrix} 0.036 & -0.004 & -0.002 \\ -0.004 & 0.016 & -0.004 \\ -0.002 & -0.004 & 0.008 \end{bmatrix},$$

test the above hypothesis;

- (c) assume that White's heteroskedasticity test accepts its null hypothesis, and that the robust estimate of the coefficient covariance matrix is

$$\tilde{V} = \begin{bmatrix} 0.044 & -0.003 & -0.002 \\ -0.003 & 0.022 & -0.001 \\ -0.002 & -0.001 & 0.005 \end{bmatrix}.$$

Do your conclusions change?